B-series and TSRK pairs based on Gaussian quadratures

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Abstract.

Solutions to non-stiff or mildly-stiff initial value systems of ordinary differential equations may be approximated **efficiently** by explicit Runge–Kutta pairs or linear multistep methods. Hybrid explicit two-step Runge–Kutta pairs have been designed in an attempt to improve on efficiency/accuracy benefits of such treatments. Here, a B-series approach is used to characterize the order conditions for TSRK methods, previously derived using an algebraic approach by Butcher and Tracogna. This leads to the construction of a MAPLE code which may be used to verify the order of particular methods, and compute norms of the local truncation error coefficients. The latter may be used as a criteria for searching for and selecting good algorithms.

Recent work establishes an alternative formulation for representing the order conditions using a recursion based on Butcher's theory. This leads to a restricted sub-family of pairs based on weights from Lobatto and Radau quadrature rules which simplifies trequired starting methods and allows for easy change of stepsize. Results using order six pairs will be presented.