MATH 232 98-2 MIDTERM 1 ANSWER KEY

QUESTION	Answer	Max	SCORE
1	[10, -2, 7]	3	
2	$oldsymbol{w} = oldsymbol{v} - oldsymbol{u}$	4	
3	$x_1 \begin{bmatrix} 3 \\ 0 \\ 4 \end{bmatrix} + x_2 \begin{bmatrix} -1 \\ 2 \\ -2 \end{bmatrix} + x_3 \begin{bmatrix} 4 \\ -5 \\ 1 \end{bmatrix} = \begin{bmatrix} 9 \\ -12 \\ 10 \end{bmatrix}$	4	
4	(a) $oldsymbol{u}$ (b) $oldsymbol{u}$ and $oldsymbol{x}$	2 2	
5	$ \left[\begin{array}{cccc} 1 & 0 & 4/5 & 0 \\ 0 & 1 & 7/5 & -1 \\ 0 & 0 & 0 & 0 \end{array}\right] $	5	
6	$\boldsymbol{x} = \begin{bmatrix} 2 \\ 0 \\ -2 \\ 0 \end{bmatrix} + a \begin{bmatrix} -3 \\ 1 \\ 0 \\ 0 \end{bmatrix} + b \begin{bmatrix} 1 \\ 0 \\ -5 \\ 1 \end{bmatrix} \qquad (a, b \in \mathbb{R})$	5	
7	$A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$	5	
8	$\{[-5,-2,1,0],[3,1,0,1]\}$	5	
9	Yes, vectors are a basis of their span No, they are not x Brief reason: the reduced row-echelon form of $\begin{bmatrix} \boldsymbol{v}_1^T & \boldsymbol{v}_2^T & \boldsymbol{v}_3^T \end{bmatrix}$ does not have a pivot in every column; alternatively, observe that $4\boldsymbol{v}_1 - 3\boldsymbol{v}_2 - \boldsymbol{v}_3 = \boldsymbol{0}$.	5	

Total	
-------	--