Math 303, Fall 2011, Lecture 13

D The Lian's paradox

This sentence is false.

If it is tree then

If it is false the

We can had lob of examples of presentations of this paradox









calamities of nature.com @ 2009 Tony Piro

Fred only said two things in this comic



Copyright 3 2003 United Feature Syndicate, Inc.

This one's

Self reference (a sentence talking about itself) is not necessary for the paradox

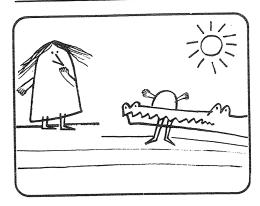
A: Sertonce B is true

B: Sentence A is false

A colleague of nine says he has a foolproof pickup line

Answer to blue grachian Answer to will you go out with me

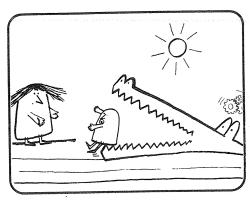
## Crocodile and Baby



Greek philosophers liked to tell about a crocodile that snatched a baby from its mother.

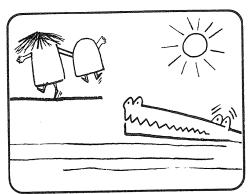
**Crocodile:** Will I eat your baby? Answer correctly and I'll give the baby back to you unharmed.

Mother: Oh! Oh! You're going to eat my baby.



Crocodile: Hmmm. What shall I do? If I give you back your baby, you will have spoken falsely. I should have eaten it. . . . Okay, so I won't give it back.

**Mother:** But you must. If you eat my baby, I spoke correctly and you have to give it back.



The poor crocodile was so freaked that it let the baby go. The mother grabbed her child and ran.

**Crocodile:** Zounds! If only she'd said I'd give the baby back. I'd have had a juicy meal.

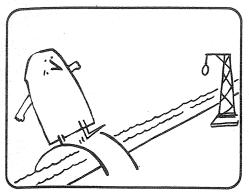
The crocodile has a problem. He has to both eat the baby and give it back, at the same time.

The mother is very clever. Suppose, instead, she had said: "You're going to give the baby back." Then, the crocodile could return the baby or eat it, in both cases without contradiction. If he gives it back, the mother spoke truly, and the crocodile has kept his word. On the other hand, if he is mean enough, he can eat the baby. This makes the mother's statement false, which frees the crocodile from the obligation to give the baby back.

Mother's	Crocodile's action	Paradox?

From Aha Gotcha by Markin Gardner

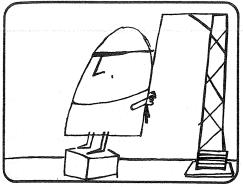
## The Don Quixote Paradox



The novel Don Quixote tells of an island with a curious law. A guard questions every visitor:

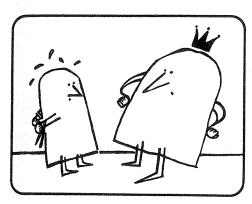
**Guard:** Why are you coming here? If the visitor answers truly,

all is well. If he answers falsely he is hanged.



One day a visitor answered: **Visitor:** I came here to be hanged!

The guards were as puzzled as the crocodile. If they do not hang the man, he has lied and has to hang. But if they hang him, he spoke truly and should not be hanged.



To decide the matter, the visitor was taken to the island's governor. After thinking long and hard the governor made his decision. **Governor:** Whatever I decide is sure to break the

law. So I will be merciful and let the man go free.

The hanging paradox is in Chapter 51 of the second book of *Don Quixote*. Sancho Panza, the Don's servant, has become governor of an island where he has sworn to uphold the country's curious law about visitors. When the visitor is brought before him, he decides the man's case with mercy and common sense.

The paradox, although similar to the crocodile paradox, is clouded by the ambiguity of the visitor's statement. Is it the man's statement about his intent, or is it a statement about a future event? In the first sense, the man may have spoken truly about his intent, and the authorities could then not hang him and there would be no contradiction. But if his statement is taken in the second sense, then whatever the authorities do will contradict the law.

From Aha Gotcha by Markin Gardner

How do revolve the liar's paradox?

Taroki's Metalanguageo

Or naybe

Gödel's first in completeness theorem says that if a formal teary is a strong enough to express elementary with metic then there are true statements about arithmetic which are not provable within the theory He shows this by expressing the statement This statement is unprovable in arithmetic in the formal theory

2) Next time

- Predicate calculus (the rest of the rules for our system)

- The axioms of set heavy
expressed in first order logic

Please read Cohen ch II section 1